



Structural coregraph of triple layered fuzzy graph

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Abstract

In this dissertation we discussed the basic concepts of double layered fuzzy graph, triple layered fuzzy graph, fuzzy distance, and spanning tree.

Fuzzy graph theory was introduced by Ariel Rosenfeld in 1975. Though it is very Young, it has been growing fast and has numerous applications in various fields. During the same time Yeh and Bang have also introduced various concepts of connectedness in fuzzy graphs.

The degree of a vertex in fuzzy graphs which are obtained from two given fuzzy graphs using operations were discussed by Nagoor Gani and Radha. Radha and Kumaravelintroduced the concept of degree of an edge and total degree of an edge in fuzzy graphs.

We study the degree of an edge in fuzzy graphs which are obtained from two given fuzzy graphs using the operations of union and join. In general, the degree of an edge in union and join of two fuzzy graphs G_1 and G_2 cannot be expressed in terms of these in G_1 and G_2 .

Keywords: fuzzy graphs, by Nagoor Gani, degree of an edge, core graph

Introduction

Fuzzy graph theory was introduced by Rosenfeld in 1975 [5]. The degree of a vertex in some fuzzy graphs was discussed by Nagoorgani and Radha [7]. Nagoorgani and Malarvizhi have defined different types of fuzzy graphs and discussed its relationships with isomerism in fuzzy graphs [3]. The double layered fuzzy graph was introduced by Pathinathan and Jesintha Rosline, they have examined some of the properties of DLFG [4].

In this paper, Mrs. L. Jethruth Emelda Mary and P. Amutha introduced the structural core graph of Triple Layered Fuzzy Graph Using new algorithm.

3.2: Structural Core Graph

In this section, we have introduced new algorithm to construct a structural core graph of Triple Layered Fuzzy Graph. (i.e) To obtain a spanning tree for the given Triple Layered Fuzzy Graph.

Algorithm 3.3

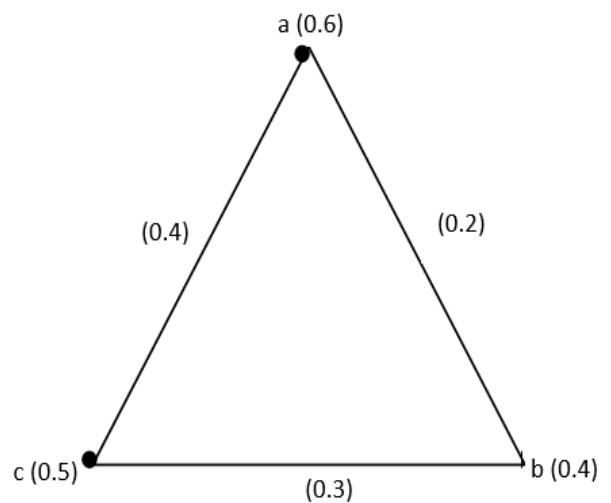
1. Construct a TLFG with $3n$ vertices and $5n$ edges where n is the number of vertex in the base graph whose crisp graph is cycle.
2. Calculate face values using the formulae. $\text{Min} \frac{\mu(a,b)}{\sigma(a) \wedge \sigma(b)}$ where $\mu(a, b)$ is the weight of the edge (a, b) and $\sigma(a) \wedge \sigma(b)$ are membership value of vertices a and b in TLFG.
3. Select a face with least value. If two (or) more faces are there with least value, choose a face with least order value.
4. Choose a vertex with least value in the selected face.
5. Select the smallest fuzzy distance, fuzzy distance

edge from the selected vertex and include that in T . If two (or) more edges are there with the same value choose an edge with least adjacent vertex value, where T is a tree of TLFG.

6. If two (or) more vertices are there with same value then choose the edge with least intersecting face value.
7. Repeat this procedure till we cover all the vertices of TLFG.
8. Stop, when T becomes Spanning tree of TLFG.

Example 3.4

Consider a fuzzy graph $G: (\sigma, \mu)$ with $n=3$ vertices whose crisp graph is a cycle C_3 .



Example: 3.5

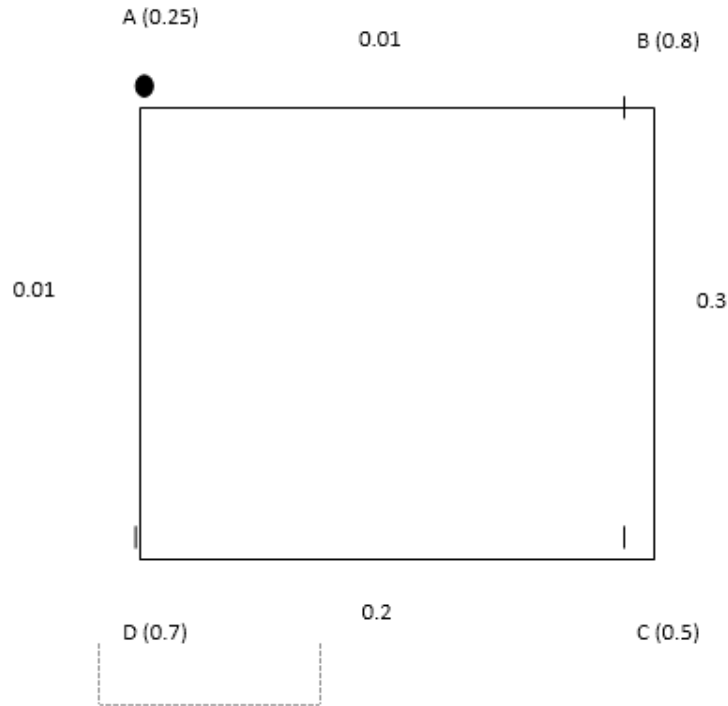


Fig 4: Fuzzy graph (C₄)

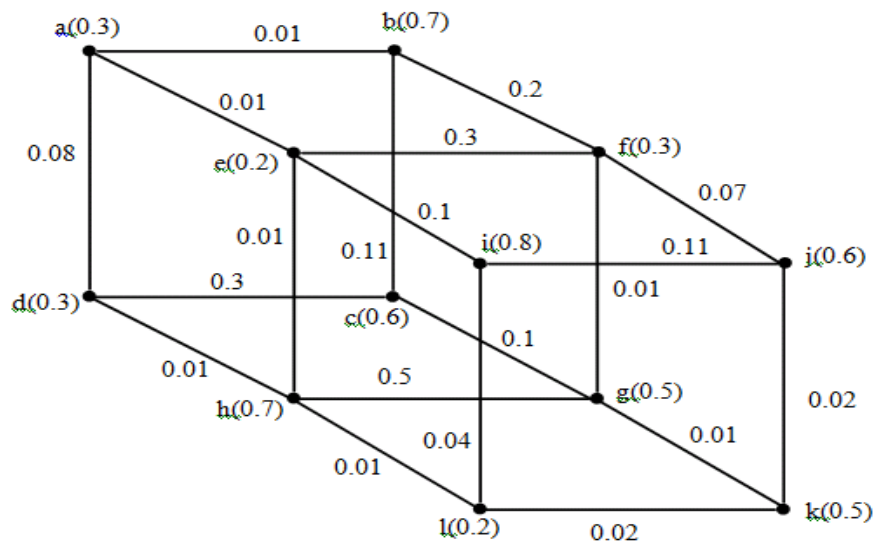


Fig 5: TLFG of n = 4 vertices

Facevalue calculation

- $F_1(a b c d) \rightarrow \min \{0.03, 0.18, 1, 0.26\} = 0.03$
- $F_2(e f g h) \rightarrow \min \{1, 0.03, 1, 0.02\} = 0.02$
- $F_3(i j k) \rightarrow \min \{0.2, 0.18, 0.04, 0.02\} = 0.04$
- $F_4(a e h d) \rightarrow \min \{0.03, 0.02, 0.03, 0.26\} = 0.02$
- $F_5(a e f b) \rightarrow \min \{0.03, 1, 0.66, 0.03\} = 0.03$

- $F_6(f j l g) \rightarrow \min \{1, 0.4, 1, 0.33\} = 0.33$
- $F_7(h g k l) \rightarrow \min \{1, 0.02, 0.25, 0.1\} = 0.02$
- $F_8(a b f e) \rightarrow \min \{0.03, 0.66, 1, 0.33\} = 0.03$
- $F_9(e f j i) \rightarrow \min \{1, 0.23, 0.18, 0.14\} = 0.14$
- $F_{10}(b c g f) \rightarrow \min \{0.18, 0.4, 0.03, 0.66\} = 0.03$
- $F_{11}(f j k g) \rightarrow \min \{0.23, 0.04, 0.03, 0.03\} = 0.03$

Table 2

Reached node	Edge	Membership Value	Iteration
L	Lk	0.05	1
lk	kg	0.01	2
lkg	gh	0.01	3
lkgh	hl(form cycle)	-	No
lkgh	hd	0.01	4

lkg hd	dc	0.3	5
lkg hdc	cg(form cycle)	-	No
lkg hdc b	cb	0.11	6
lkg hdc b f	bf	0.2	7
lkg hdc b f e	fg(form cycle)	-	No
lkg hdc b f e i	fe(form cycle)	-	No
lkg hdc b f e i j	ei	0.3	8
lkg hdc b f e i j k	ij	0.1	9
lkg hdc b f e i j k l	jf(form cycle)	-	No
lkg hdc b f e i j k l	jk(form cycle)	-	No
lkg hdc b f e i j k l	Ji	0.11	10
lkg hdc b f e i j k l	il(form cycle)	-	No
lkg hdc b f e i j k l	Ie	0.1	11
lkg hdc b f e i j k l	eh(form cycle)	-	No
lkg hdc b f e i j k l	ea	0.01	12
lkg hdc b f e i j k l	ad(form cycle)	-	No
lkg hdc b f e i j k l	ab	0.01	13
lkg hdc b f e i j k l	bf(form cycle)	-	No
lkg hdc b f e i j k l	fe(form cycle)	-	No
lkg hdc b f e i j k l	bc	0.11	14

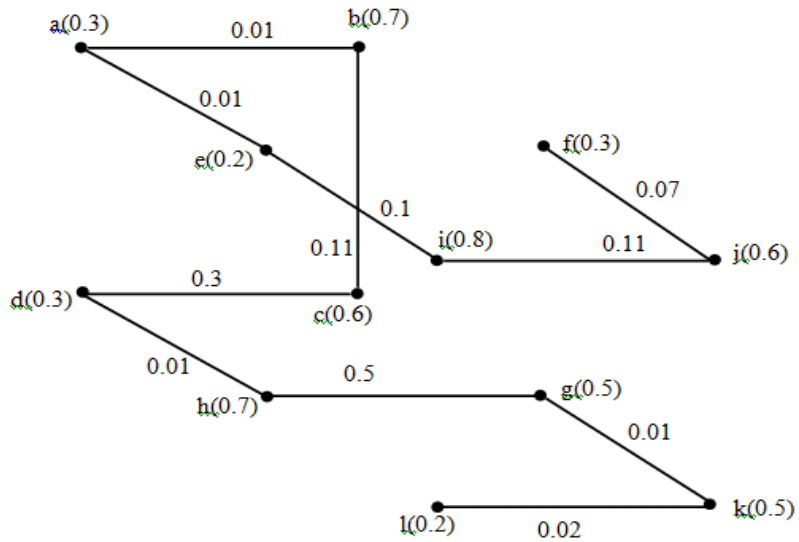


Fig 6: Structural core graph of TLFG of n=4 vertices

Example 3.6

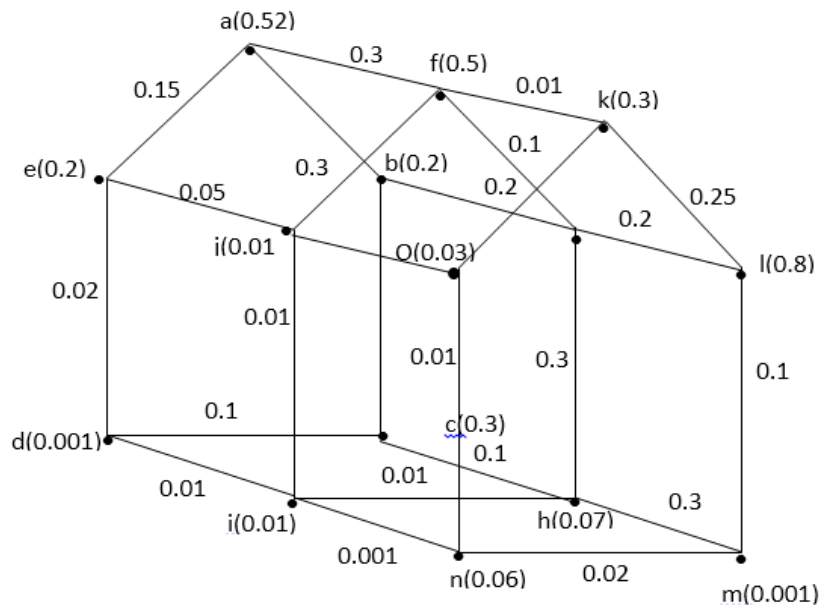


Fig 7: TLFG of order n=5 vertices

Facevalue calculation

- F₁ (a b c d e) → min {0.576, 1, 0.33, 0.1, 0.75} = 0.33
- F₂ (f g h I j) → min {0.2, 0.75, 1, 1, 1} = 0.2
- F₃ (k l m n o) → min {0.833, 0.2, 0.33, 0.16, 1} = 0.16
- F₄ (a f j e) → min {0.6, 1, 0.25, 0.75, 0.6} = 0.25
- F₅ (f k o j) → min {0.3, 1, 0.66, 1,} = 0.03

- F₆ (e j I d) → min {0.25, 1, 1, 0.1} = 0.1
- F₇ (j o n i) → min {0.66, 0.16, 0.1, 1} = 0.1
- F₈ (b g h c) → min {1, 0.75, 0.33, 1} = 0.33
- F₉ (g l m h) → min {0.28, 0.2, 0.75, 0.75} = 0.2
- F₁₁ (a f g b) → min {0.6, 0.2, 1, 0.5} = 0.2
- F₁₂ (f k l g) → min {0.33, 0.83, 0.28, 0.2} = 0.2

Table 3

Reached node	Edge	Membership Value	Iteration
I	In	0.001	1
in	nm	0.02	2
inm	mh	0.3	3
inmh	hi(form Cycle)	—	No
inmh	hc	0.1	4
inmhc	cd	0.1	5
inmhcd	di (Form Cycle)	—	No
inmhcdi	ij	0.01	6
inmhcdij	je	0.05	7
inmhcdije	ed(form cycle)	—	No
inmhcdije	ea	0.15	8
inmhcdijea	ab	0.1	9
inmkcdijea	bc(form cycle)	—	No
inmhcdijea	bg	0.2	10
inmhcdijea	gh(form cycle)	—	No
Inmhcdijea	gi	0.2	11
Inmhcdijea	Im(form cycle)	—	No
Inmhcdijea	Ik	0.25	12
Inmhcdijea	Kf	0.01	13
Inmhcdijea	fg(form cycle)	—	No
Inmhcdijea	fa	0.3	14
Inmhcdijea	ab(form cycle)	—	No
Inmhcdijea	fk(form cycle)	—	No
Inmhcdijea	fj	0.3	15

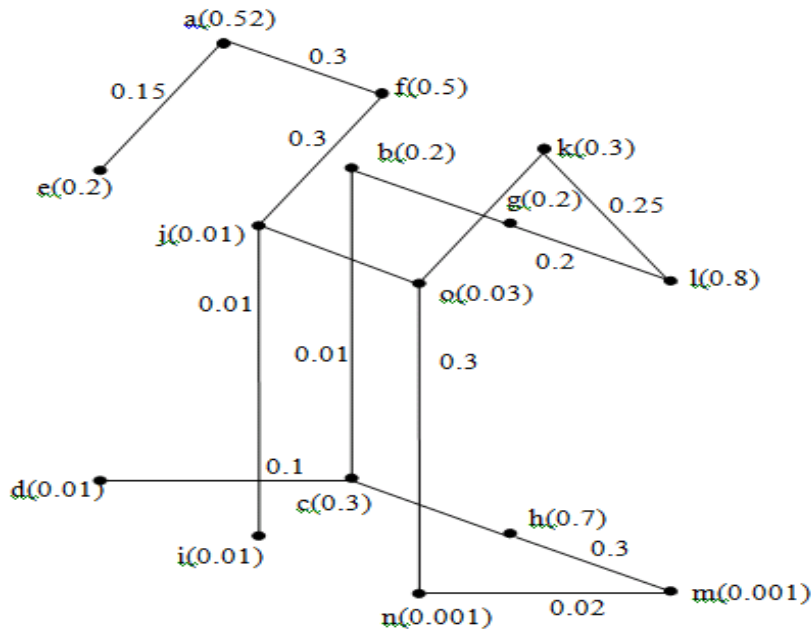


Fig 8: Structural core graph of TLFG of order n=5 vertices.

For different values of n, we will get different TLFG and when we apply the algorithm we will get different structures for each graph.

4. Theoretical Concepts

Consider the TLFG from example 3.4 with different labeling

Face value calculation

- $F_1(a\ b\ c\ d) \rightarrow \min \{0.75, 0.6, 0.4, 0.02\} = 0.02$
- $F_2(a\ x\ y\ b) \rightarrow \min \{0.8, 0.5, 0.5, 0.75\} = 0.5$
- $F_3(b\ l\ k\ c) \rightarrow \min \{0.33, 0.5, 0.02, 0.75\} = 0.02$
- $F_4(b\ y\ z\ i) \rightarrow \min \{0.4, 0.66, 0.66, 0.33\} = 0.33$
- $F_5(x\ a\ d\ h\ e) \rightarrow \min \{0.8, 0.02, 0.3, 1, 0.33\} = 0.02$

- $F_6(y\ f\ g\ c\ b) \rightarrow \min \{0.1, 0.5, 1, 0.75, 0.5\} = 0.1$
- $F_7(z\ j\ l\ k\ i) \rightarrow \min \{1, 1, 0.6, 0.5, 0.66\} = 0.5$
- $F_8(e\ f\ g\ h) \rightarrow \min \{0.1, 0.5, 0.75, 1\} = 0.5$
- $F_9(f\ j\ l\ g) \rightarrow \min \{0.5, 1, 0.6, 0.5\} = 0.5$
- $F_{10}(d\ h\ g\ c) \rightarrow \min \{0.3, 0.75, 1, 0.4\} = 0.3$
- $F_{11}(c\ g\ l\ k) \rightarrow \min \{1, 0.6, 0.6, 0.02\} = 0.02$

Table 4

Reached node	Edge	Membership Value	Iteration
I	In	0.001	1
in	nm	0.02	2
inm	mh	0.3	3
inmh	hi(form Cycle)	—	No
inmh	hc	0.1	4
inmhc	cd	0.1	5
inmhcd	di (Form Cycle)	—	No
inmhcdi	ij	0.01	6
inmhcdij	je	0.05	7
inmhcdije	ed(form cycle)	—	No
inmhcdije	ea	0.15	8
inmhcdijea	ab	0.1	9
inmkcdijeab	bc(form cycle)	—	No
inmhcdijeab	bg	0.2	10
inmhcdijeabg	gh(form cycle)	—	No
Inmhcdijeabg	gi	0.2	11
Inmhcdijeabgi	Im(form cycle)	—	No
Inmhcdijeabgi	lk	0.25	12
Inmhcdijeabgi	Kf	0.01	13
Inmhcdijeabgik	fg(form cycle)	—	No
Inmhcdijeabgikf	fa	0.3	14
Inmhcdijeabgikf	ab(form cycle)	—	No
Inmhcdijeabgikfa	fk(form cycle)	—	No
Inmhcdijeabgikfaf	fj	0.3	15

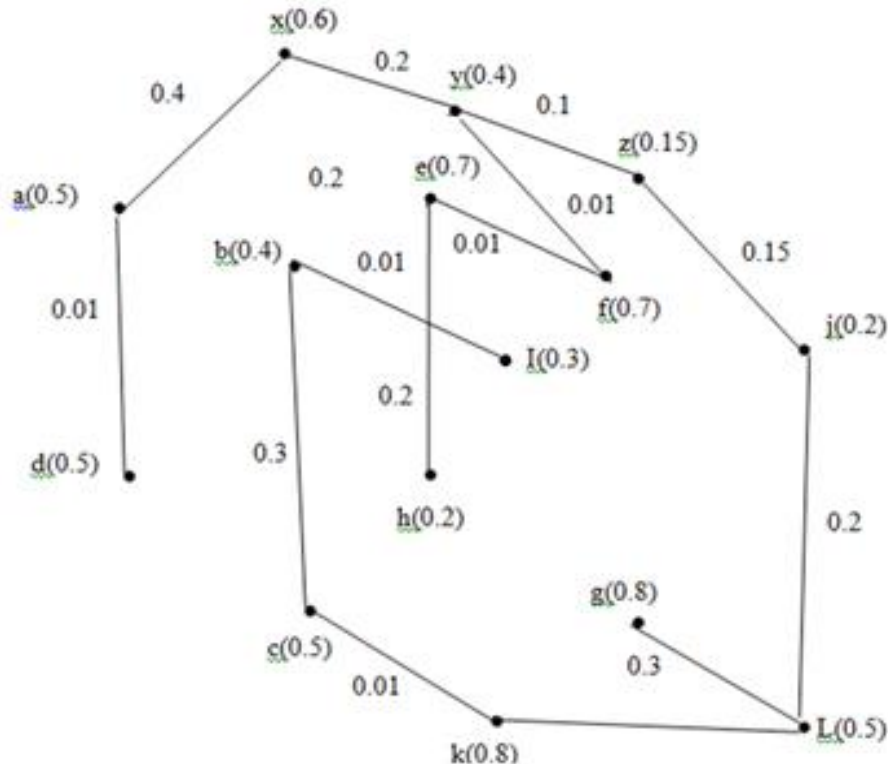


Fig 12: Structural core graph of TL (G₁) UTL (G₂)

Conclusion

In this dissertation we discussed the concept of

“The structural core graph of triple layered fuzzy graph” we obtained the optimal tree for the triple layered fuzzy graph

of order $n= 3,4,5,6,7,& 8$ using the concept of structural core graph of triple layered fuzzy graph.

This work can be entered other different layered fuzzy graph using structural core graph.

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